

Sl. No. of Ques. Paper : 401 C
Unique Paper Code : 222181
Name of Paper : Physics – I
Name of Course : B.Sc. (Hons) Maths. / B.Sc. (Mathematical Science)
Semester : I
Duration : 3 hours

Maximum Marks : 75

Attempt five questions in all. Question No. 1 is compulsory. Select at least two questions from each of Sections A and B.

- 1 Attempt any five: 3x5=15
- (a) Determine a unit vector perpendicular to plane containing
 $\mathbf{a} = 2\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}$
 $\mathbf{b} = 4\mathbf{i} + 3\mathbf{j} - \mathbf{k}$
 - (b) Prove: $(\mathbf{A} \times \mathbf{B}) \cdot (\mathbf{C} \times \mathbf{D}) = (\mathbf{A} \cdot \mathbf{C})(\mathbf{B} \cdot \mathbf{D}) - (\mathbf{B} \cdot \mathbf{C})(\mathbf{A} \cdot \mathbf{D})$
 - (c) Show that gradient of field describing motion is irrotational
 - (d) $\text{div}(s\mathbf{A}) = s \text{div}\mathbf{A} + \mathbf{A} \cdot \text{grad } s$
 - (e) Show that $\mathbf{A} = (6xy + z^3)\mathbf{i} + (3x^2 - z)\mathbf{j} + (3xz^2 - y)\mathbf{k}$ is irrotational.
 - (f) Show that $\mathbf{F} = (2xy + z^3)\mathbf{i} + x^2\mathbf{j} + 3xz^2\mathbf{k}$ is a conservative force field. Find the scalar potential
 - (g) State Stokes' theorem. Write it in rectangular form.

Section A

- 2 (a) Find the resultant of two S.H.M. of equal period, when they are perpendicular to one another. Discuss different cases. 10
- (b) A mass of 25×10^{-3} kg is suspended from the lower end of the vertical spring having a force constant 25 N/m. The mechanical resistance of the system is 1.5 N/m. The mass is displaced vertically and released. Find whether the motion is oscillatory? If so calculate the period of oscillation. 5
- 3 (a) Define moment of inertia. State and prove theorem of perpendicular axis. 5

- 10
- (b) Find the moment of inertia of an annular circular lamina about an axis along its diameter.
- 4 (a) What are elastic and inelastic collision? Discuss elastic collision in one dimension for two particles. 6
- (b) A particle of mass m_1 experiences a perfectly elastic collision with a stationary particle of mass m_2 . Determine the ratio of m_1/m_2 if after a headon collision the particles fly apart in opposite directions with equal velocities. 5
- (c) Calculate the group velocity when the two waves

$$Y_1 = 10 \sin (2\pi t - 5x)$$

$$Y_2 = 15 \sin (5\pi t + 5x)$$
 Superimpose. Y_1 and Y_2 are in meters. 4

Section B

- 5 (a) What is interference? Give the necessary conditions to obtain sustainable and discernable interference fringes. 1+4
- (b) Derive an expression for optical path difference in thin films due to reflected light. Obtain the conditions for maxima and minima. 4+4
- (c) Explain the colours in thin films. 2
- 6 (a) Distinguish between Fresnel and Fraunhofer class of diffraction. 2
- (b) Give construction and theory of plane transmission grating. Discuss the intensity distribution. 7+3
- (c) Show that the resolving power of grating is proportional to the order of diffraction. 3
- 7 (a) What do you understand by polarization of light? How do you obtain plane polarized light by reflection and refraction? 1+6
- (b) State and explain Brewster's Law. 2
- (c) What are quarter and half wave plates? Discuss one application of each. 6