

This question paper contains 2 printed pages.

Your Roll No.

Sl. No. of Ques. Paper : 8309 C
Unique Paper Code : 222161
Name of Paper : PHPT-101 : Physics – I Mechanics
Name of Course : B.Sc. Physical Science / Applied Physical Science Part I
Semester : I
Duration : 3 hours

Maximum Marks : 75

Attempt five questions in all. Question No. 1 is compulsory.

Attempt four questions from the rest of the paper.

1. Attempt any five of the following:

5 × 3 = 15

- (a) If $\vec{A} = 3xyz^2\hat{i} + 2xy^3\hat{j} - x^2yz\hat{k}$ and $\phi = 3x^2 - yz$, find the value of $\vec{\nabla} \cdot (\phi \vec{A})$.
- (b) The potential energy of a particle is described by $U = A \log_e(x^2 + y^2 + z^2)$. What will be the force acting on the particle?
- (c) Explain the physical significance of the negative results of the Michelson-Morley experiment.
- (d) How fast should a spaceship move relative to an observer on earth, in order that one year on it may correspond to two years on earth?
- (e) The maximum and minimum distances of a planet from the sun are 2.8×10^8 km and 1.4×10^8 km, respectively. Calculate the magnitude of its velocity when the planet is nearest to the sun, if the velocity when it is farthest is 3×10^3 m/s.
- (f) Define impulse. A cricket ball of mass 100 g moving with a velocity of 12 m/s is hit by a bat, so that it is turned back with a velocity of 20 m/s. The force of the blow acts for 0.01 second on the ball. Find the average force exerted by the bat on the ball.
- (g) State Kepler's laws of planetary motion.

2. (a) What is centre of mass? Show that in the absence of external forces, the velocity of the centre of mass remains constant. **10**

(b) Show that law of conservation of momentum is invariant to Galilean transformation. **5**

3. (a) Define moment of inertia for a rigid body. A flywheel of mass 500 kg, radius 1 m makes 500 revolutions per minute. Assuming the mass to be concentrated along the rim, calculate the energy of the flywheel. 5
- (b) Calculate the moment of inertia for a solid cylinder of mass M , length L and radius R about an axis passing through its centre and perpendicular to its length. 10
4. (a) Explain what is meant by modulus of rigidity of a material. Obtain an expression for the couple per unit twist for a wire having circular cross-section. 10
- (b) Show that under the influence of a central force, angular momentum of a particle is conserved and its motion is confined to a fixed plane. 5
5. (a) State and prove Green's theorem in a plane. 10
- (b) Prove
$$\iint_S r^5 \hat{n} ds = \iiint_V 5r^3 \vec{r} dV$$
 5
6. (a) Deduce an expression for relativistic variation of mass with velocity. 10
- (b) What are massless particles? Show that they exist only if they move with the speed of light. 5
7. (a) Write Lorentz transformation equations and use them to derive an expression for length contraction. 10
- (b) Determine the length of a rod of proper length 1 m with respect to an observer moving with a velocity $0.8c$ in a direction inclined at 30° to its length. 5
8. (a) Show that $\vec{\nabla} \phi$ is a vector perpendicular to the surface $\phi(x, y, z) = c$, where c is a constant. 5
- (b) In what direction from the point $(1, 3, 2)$ is the directional derivative of $\phi = 2xz - y^2$ a maximum? What is the magnitude of this maximum? 5
- (c) Evaluate $\oint (y - 2x)dx + (3x + 2y)dy$ around the boundary of a circle of unit radius centered at origin. 5