

*This question paper contains 3 printed pages.*

8471

Your Roll No. ....

**B.Tech. / I**

**A**

PAPER EEE/EEC-101

MATHEMATICS – I

Time : 3 hours

Maximum Marks : 70

*(Write your Roll No. on the top immediately  
on receipt of this question paper.)*

*Attempt any five questions.*

*All questions carry equal marks.*

*Assume missing data suitably, if any.*

1. (a) Discuss the convergence of the series:

(i)  $\sum(\sqrt{n^4+1})-\sqrt{n^4-1}$

(ii)  $x - \frac{x^2}{2^2} + \frac{x^3}{3^2} - \frac{x^4}{4^2} + \dots$

(b) If  $\alpha, \beta$  are the roots of  $x^2 - 2x + 4 = 0$ , prove that

$$\alpha^n + \beta^n = 2^{n+1} \cos \frac{n\pi}{3}.$$

2. (a) Obtain the eigen values and eigen vectors for the matrix:

P. T. O.

$$\begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{bmatrix}.$$

Verify that the eigen vectors are orthogonal.

(b) If  $y^{1/m} + y^{-1/m} = 2x$ , prove that:

$$(x^2 - 1)y_{n+2} + (2n+1)xy_{n+1} + (n^2 - m^2)y_n = 0.$$

3. (a) Calculate the approximate value of  $\sqrt{10}$  to four places of decimal by taking the first four terms of an appropriate expansion.

(b) Find the half-range cosine and sine series for the function:

$$f(x) = x(\pi - x), \quad 0 \leq x \leq \pi.$$

4. Solve:

$$(a) \quad \frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + \frac{dy}{dx} = e^{2x} + x^2 + x$$

$$(b) \quad \frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = x \sin x$$

5. (a) Evaluate  $\iint_A xy \, dx \, dy$ , where  $A$  is the domain bounded by  $x$ -axis, ordinate  $x=2a$  and the curve  $x^2=4ay$ .

(b) Evaluate:

$$\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} \frac{1}{\sqrt{1-x^2-y^2-z^2}} dz dy dx.$$

6. (a) Trace the curve:

$$3ay^2 = x(x-a)^2$$

(b) Find the area of ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

7. (a) Show that for the cardioid

$$r = a(1 + \cos \theta),$$

$$\frac{\rho^2}{r} \text{ is constant.}$$

(b) Find the asymptotes of the curve:

$$x^3 + 4x^2y + 5xy^2 + 2y^3 + 2x^2 + 4xy + 2y^2 - x - 9y + 2 = 0$$