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**Unique Paper Code : 2511504**

**Name of the Paper : Numerical Methods**

**Name of the Course : B. Tech. Electronics**

**Semester : V**

F-5

**Duration : 3 Hours**

**Maximum Marks: 75**

**Instructions for Candidates**

Q. No. 1 is Compulsory

Attempt Five Questions in all

All questions carry equal marks.

Non-programmable scientific calculators are allowed.

- 1 Attempt ALL.
- (a) Find the sum of  $0.123 \times 10^3$  and  $0.456 \times 10^2$  and write the result in three digit mantissa form.
- (b) Define accuracy, absolute error and relative error.
- (c) Compare Newton Raphson and secant in terms of convergence, number of function evaluation per iteration and accuracy.
- (d) Find the inverse of the matrix using Gauss Jordan method
- $$A = \begin{bmatrix} 1 & 3 \\ 2 & 7 \end{bmatrix}$$
- (e) Given  $f(0) = -1$ ,  $f(1) = 1$  and  $f(2) = 4$ , find the Newton's interpolating formula.

5 x 3 = 15

- 2(a) Find the root of an equation  $x^3 - 5x + 1 = 0$  correct up to 3 significant digits using Regula Falsi in the interval  $[2, 3]$ . Also explain its graphical interpretation and specify the number of iterations in which solution is reached.

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- (b) Perform three iterations of the bisection method and obtain the smallest positive root of the equation in the interval  $[0, 1]$ .

$$x^3 + 2x - 2 = 0$$

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- 3(a) Solve the following system of equations using Gauss elimination method.

$$2x + 6y + 10z = 0$$

$$x + 3y + 3z = 2$$

$$3x + 14y + 28z = -8$$

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- (b) Solve the following system of equations using the Gauss Seidel method

$$8x_1 - 3x_2 + 2x_3 = 20$$

$$4x_1 + 11x_2 - x_3 = 33$$

$$x_1 + x_2 + 4x_3 = 9$$

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- 4(a) Find the polynomial using Lagrange interpolation of the given tabulated data

$x$	-2	0	2
$F(x)$	4	2	8

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- (b) In mathematics, functions can often be represented by infinite series. For example, the exponential function can be computed using

$$e^x = 1 + x + \frac{x^2}{2} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!}$$

Calculate the value of  $e^{0.5}$  after 4 terms respectively. Also give the percent

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relative error.

- (c) Define the shift operator ( $E$ ), forward difference operator ( $\Delta$ ), backward difference operator ( $\nabla$ ) also derive the following relationships:

- i.  $\Delta \cdot \nabla = \Delta - \nabla$
- ii.  $\nabla = \frac{E-1}{E}$
- iii.  $\Delta = E-1$

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- 5(a) Give two characteristics of Cubic Spline interpolation. Fit the following points by cubic spline interpolation using the initial conditions

$$M_0 = M_3 = 0.$$

$X$	0	1	2	3
$Y$	1	2	33	244

Estimate the function at  $x=2.5$ .

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- (b) Derive the Trapezoidal rule of Integration for  $n$  points. Also explain its limitations.

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- 6(a) Find the first and second derivative of  $f(x)$  at  $x=1.5$  from the following tabulated values

$x$	$f(x)$
1	3.23
1.5	3.19
2	3
2.5	2.91
3	2.81

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- (b) Evaluate  $\int_0^1 \left( \frac{1}{1+x} \right) dx$  correct up to three decimal place using Simpson's  $\frac{1}{3}$  Rule of Integration with  $n=6$ .

Also find relative and percentage error w.r.t. true value.

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- 7 (a) Using Euler method find the approximate value of  $y$  when  $x=0.4$

$$\frac{dy}{dx} = x + y^2$$

when  $y(0)=1$  and  $h=0.1$ .

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- (b) Using Runge Kutta method of fourth order find  $y(0.1)$  and  $y(0.2)$ ; given that  $\frac{dy}{dx} = 1 + xy$ , with the initial condition of  $y(0)=2$ .

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